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Welcome!

Physics 194 - Lecture 13

Have a question during class? Please ask it right away, even if it means interrupting in the middle of a thought. I want you to!

Agenda

- Frequency
- Kinematics of vibrational motion
- Pendulums

Class
starts
@ 2:15 pm

Vibrational motion (type of periodic motion)

Equilibrium position



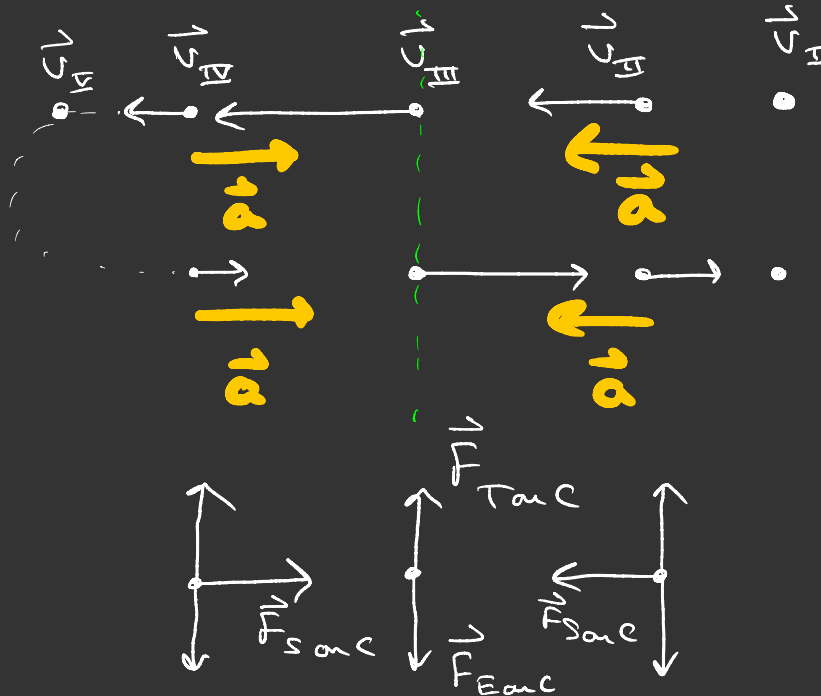
The period of motion is how much time one cycle of motion takes, T , in

Motion seconds. Frequency is

diagram $f = \frac{1}{T}$, and

unit is s^{-1} \rightarrow is the # of cycles that complete in each second.
= Hz (Hertz)

Force diagrams

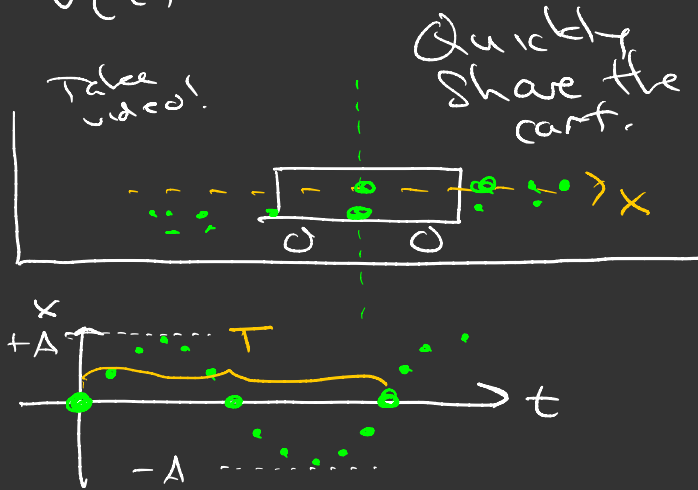


$$T = 2\pi \sqrt{\frac{m + \frac{1}{3}m_s}{k}}$$

What's the equivalent of kinematics for vibrational motion?

$$x(t) =$$

$$v(t) =$$



If an object has constant acceleration (vibrational motion doesn't)...

$$x(t) = x_0 + v_0 t + \frac{1}{2} a t^2$$

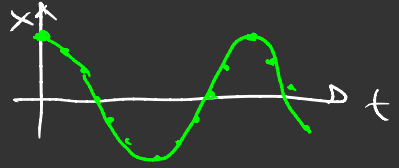
$$v(t) = v_0 + a t$$

⋮

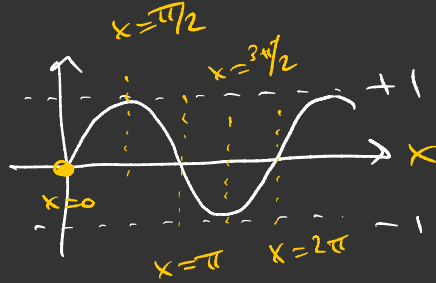
Vibrational motion needs 3 things

- 1) Equilibrium position
- 2) "Restoring force"
- 3) Add energy!

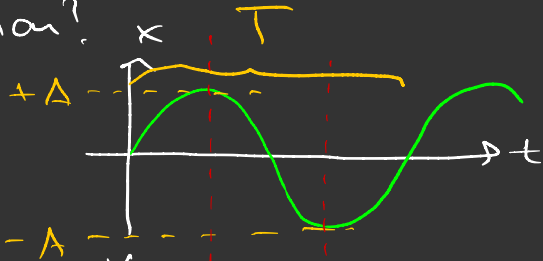
$$x(t) = \pm A \sin\left(\frac{2\pi}{T}t\right) \quad x(t) = \pm A \cos\left(\frac{2\pi}{T}t\right)$$



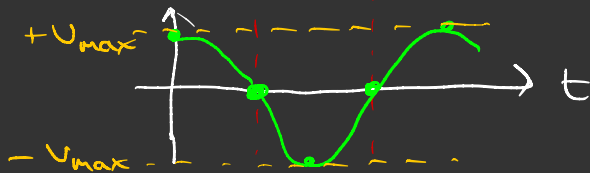
$$\begin{aligned} f(x) &= \sin(x) \\ &= \sin\left(\frac{2\pi}{T}x\right) \end{aligned}$$



What about the velocity of an object in vibrational motion?

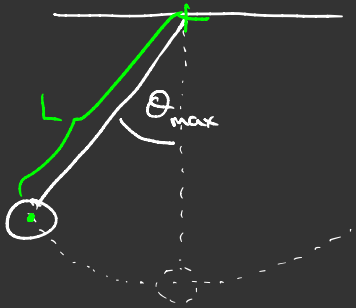


$$x(t) = A \sin\left(\frac{2\pi}{T}t\right)$$



$$v(t) = v_{max} \cos\left(\frac{2\pi}{T}t\right)$$

Pendulums



Equilibrium
position

mass of
pendulum →

Simple pendulum

- 1) Compact object attached to a "lightweight" cable
point mass!
- 2) No "dissipative" interactions
- 3) Small vibrations.

Amplitude: Max angle from equilibrium.

Period: What does it depend on?

L: When you x4 the length, the period doubles. $T \propto \sqrt{L}$

m: No dependence.

θ_{\max} : No dependence, until θ_{\max} starts getting to around $\sim 10^\circ$.

Small vibrations

$$T = 2\pi \sqrt{\frac{L}{g}}$$