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Physics 194 - Lecture 8

Welcome!

Have a question during class? Please ask it right away, even if it means interrupting in the middle of a thought. I want you to!

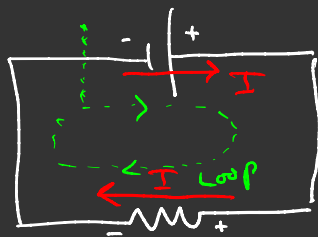
Agenda

- Multi-device circuits
- Circuit simplification + analysis
- Electrical systems in buildings

Class
starts
@ 2:15 pm

Analysis of the simplest circuit

$$\mathcal{E} = 120 \text{ V}$$



$$R = 72 \, \Omega$$

$$\sum_{\text{loop}} \Delta V = 0$$

$$\Delta V_{\mathcal{E}} + \Delta V_R = 0$$

$$+\mathcal{E} - IR = 0$$

$$I = \frac{\mathcal{E}}{R} = \frac{120 \text{ V}}{72 \, \Omega} = 1.67 \text{ A}$$

Power

$$P = I \Delta V \quad (\text{A}) \quad (\text{V})$$

$$P_R = I_R \Delta V_R = (1.67 \text{ A})(120 \text{ V})$$

$$= 200 \text{ W}$$

$$(W = J/s)$$

$$\Delta V_{\mathcal{E}} = \mathcal{E}$$

$$\Delta V_R = I_R R$$

Resistors only

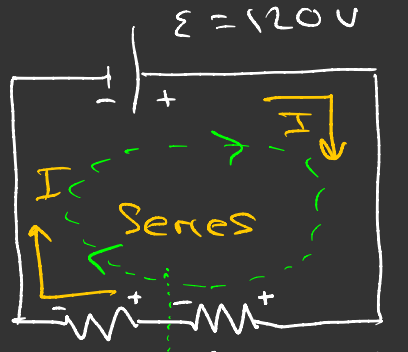
All

$$P = I \Delta V = \left(\frac{\Delta V}{R} \right) \Delta V = \frac{\Delta V^2}{R}$$
$$= I(I R) = I^2 R$$

$$\frac{\Delta V^2}{R}$$

Joule's law

Resistors only



$$R_2 = 144\ \Omega \quad R_1 = 72\ \Omega$$

$$\sum_{\text{loop}} \Delta V = 0$$

$$\Delta V_{R_2} + \Delta V_{\varepsilon} + \Delta V_{R_1} = 0$$

$$-IR_2 + \varepsilon - IR_1 = 0$$

$$\rightarrow I = \frac{\varepsilon}{R_1 + R_2} = \frac{120\text{ V}}{72\ \Omega + 144\ \Omega} = 0.56\text{ A}$$

$$P_{R_1} = I_{R_1}^2 R_1 = (0.56\text{ A})^2 (72\ \Omega) = 23\text{ W}$$

$$P_{R_2} = I_{R_2}^2 R_2 = (0.56\text{ A})^2 (144\ \Omega) = 45\text{ W}$$

~~NOT 120 V~~

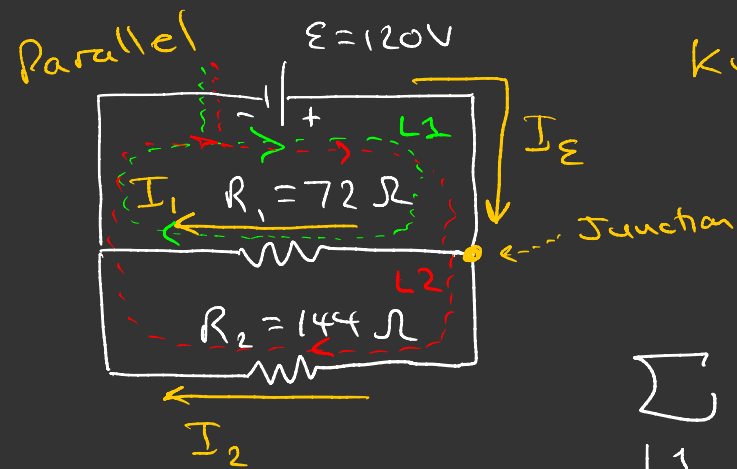
$$P_{R_2} = \frac{(\Delta V_{R_2})^2}{R_2}$$

$$= \frac{(80\text{ V})^2}{144\ \Omega} = 45\text{ W}$$

$$\Delta V_{R_2} = I_{R_2} R_2 = (0.56\text{ A})(144\ \Omega) = 80\text{ V}$$

$$\Delta V_{R_1} = I_{R_1} R_1 = (0.56\text{ A})(72\ \Omega) = 40\text{ V}$$

$$= 120\text{ V}$$



Kirchhoff's junction rule:

$$\sum I_{in} = \sum I_{out}$$

$$I_\mathcal{E} = I_1 + I_2$$

$$\sum_{L1} \Delta V = 0 \rightarrow \Delta V_\mathcal{E} + \Delta V_{R_1} = 0$$

$$+ \mathcal{E} - I_1 R_1 = 0 \rightarrow I_1 = \frac{\mathcal{E}}{R_1} = \frac{120\text{V}}{72\ \Omega}$$

$$\sum_{L2} \Delta V = 0$$

$$\Delta V_\mathcal{E} + \Delta V_{R_2} = 0$$

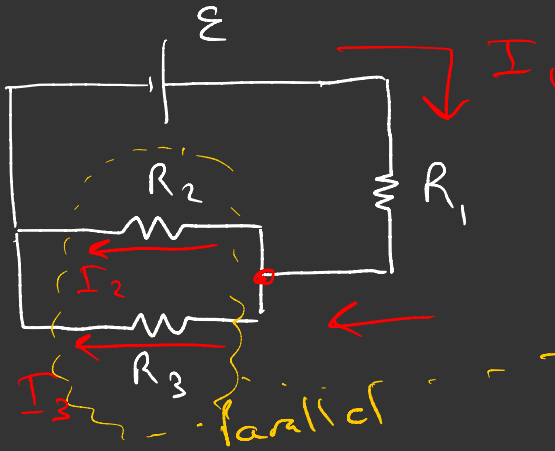
$$+ \mathcal{E} - I_2 R_2 = 0$$

$$I_2 = \frac{\mathcal{E}}{R_2} = \frac{120\text{V}}{144\ \Omega} = 0.83\text{A}$$

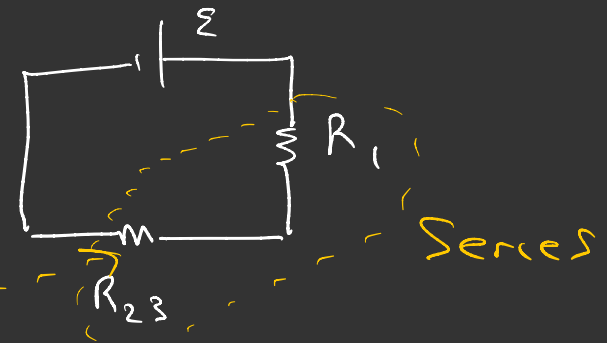
$$P_{R_1} = I_1^2 R_1 = (1.67\text{A})^2 (72\ \Omega) = 200\text{W}$$

$$I_\mathcal{E} = I_1 + I_2 = 2.5\text{A}$$

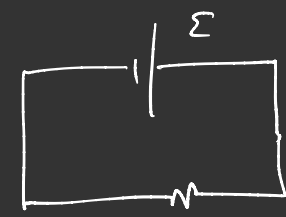
$$P_{R_2} = I_2^2 R_2 = (0.83\text{A})^2 (144\ \Omega) = 100\text{W}$$



Simplify $\rightarrow$



Simplify $\downarrow$



$$R_{123} = R_1 + R_{23}$$

-1 Series

Simplify in parallel...

$$R_{23} = \left(\frac{1}{R_2} + \frac{1}{R_3} + \dots \right)^{-1}$$

$< R_2$ and R_3

Parallel

$$R_{eq} = \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots \right)^{-1}$$

$$R_{eq} = R_1 + R_2 + R_3 + \dots$$